

Semiquantum games to verify quantum correlations (in space and in time)

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14 June 2017

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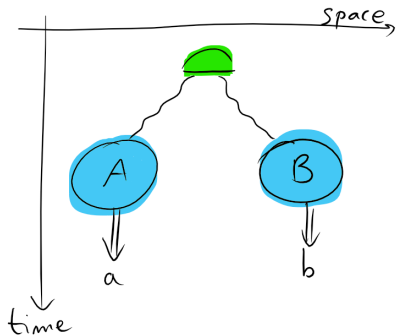


and Denis Rosset (Tainan)



Two paradigms for entanglement verification

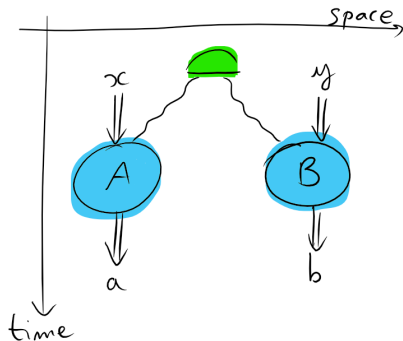
Entanglement witnesses



$$p(a, b) = \text{Tr}[(P_A^a \otimes Q_B^b) \rho_{AB}]$$

- 😊 faithfulness: for any entangled state, there exists a witness detecting it
- 😞 measurement devices need to be perfect

Bell tests

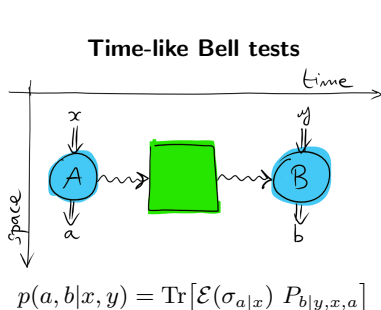
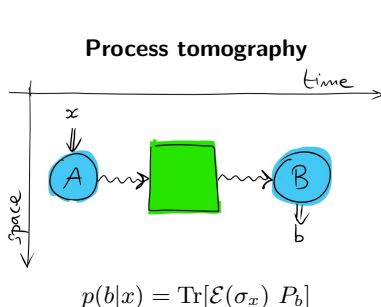


$$p(a, b|x, y) = \text{Tr}[(P_A^{a|x} \otimes Q_B^{b|y}) \rho_{AB}]$$

- 😞 hidden nonlocality: some entangled states never violate any Bell inequality
- 😊 device independence

The time-like analogue: quantum memory verification

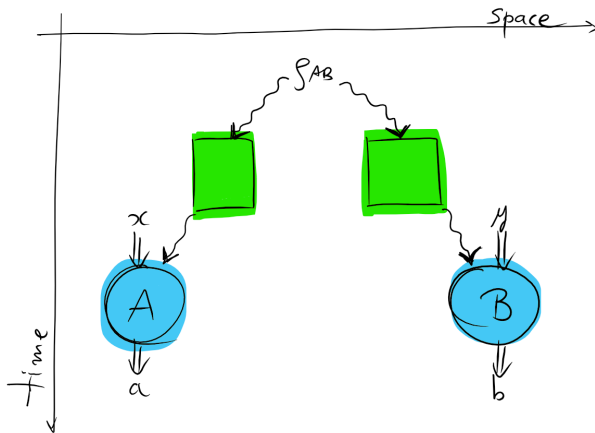
- ✓ the Choi correspondence, $\mathcal{E}_{A \rightarrow B} \longleftrightarrow \rho_{AB}$, suggests trying the same approach in time
- ✓ encouraging fact: “classical” (i.e., separable) states correspond to “classical” (i.e., entanglement-breaking) channels



- ✓ in full analogy with entanglement witnesses, process tomography is faithful (😊) but requires complete trust in the tomographic devices (☹)
- ✓ **time-like Bell tests trivialize**: A can always signal to B ($\lim_{n \rightarrow \infty} \text{☹}^{\otimes n}$)

One way around

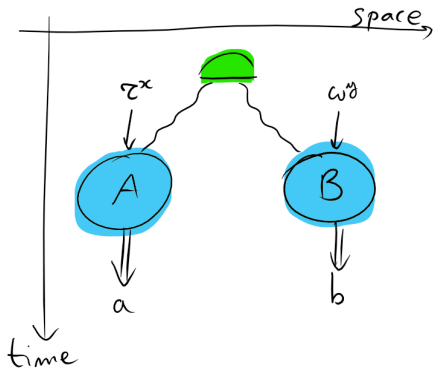
- ✓ however, if *two* quantum memories are available, one can imagine doing the following



- ✓ here, we need *two* quantum memories, and the test is assessing *the pair* simultaneously (and it's a Bell test, hence device-independent but not faithful)
- ✓ thus the problem remains: **is it possible to certify a single given memory, without using any side-channel?**

Semiquantum nonlocal games

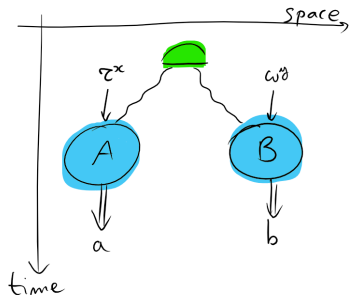
- ✓ quantum bipartite statistical decision games, a.k.a. **semiquantum games**: questions are encoded on quantum states (PRL, 2012; Editors' Suggestion and APS Physics Viewpoint)
- ✓ the referee chooses questions x and y at random
- ✓ the referee encodes questions on quantum states $\tau_{A'}^x$ and $\omega_{B'}^y$
- ✓ the system A' is sent to Alice, B' to Bob
- ✓ Alice and Bob must locally compute answers a and b
- ✓ achievable correlations are given by



$$p(a, b|x, y, \rho_{AB}) = \text{Tr} \left[(P_{A'A}^a \otimes Q_{B'B'}^b) (\tau_{A'}^x \otimes \rho_{AB} \otimes \omega_{B'}^y) \right]$$

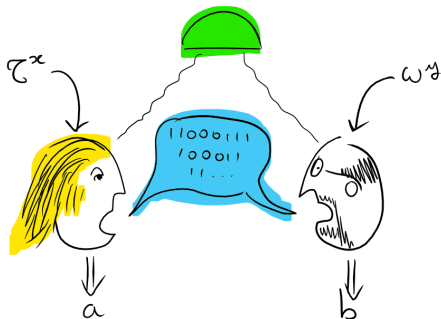
More about semiquantum nonlocal games

- ✓ usual Bell tests are recovered for distinguishable question states
- ✓ defining $\mathcal{P}(\rho_{AB}) = \{p(a, b|x, y, \rho_{AB}) \text{ for some semiquantum game}\}$, we have $\mathcal{P}(\rho_{AB}) \supseteq \mathcal{P}(\sigma_{CD})$ if and only if $\sigma_{CD} = \sum_i p_i (\mathcal{E}_A^i \otimes \mathcal{F}_B^i)(\rho_{AB})$
- ✓ namely, semiquantum games provide a complete set of monotones for the (pre-) ordering relation induced by “Local Operations and Shared Randomness” (LOSR)
- ✓ this implies faithfulness: for any entangled state, there is a semiquantum game detecting it
- ✓ interpretation as measurement-device-independent entanglement witnesses (Branciard et al., 2013; Cavalcanti et al., 2013): the referee needs to trust only the preparation devices in her lab
- ✓ two independent experimental realizations (China, Switzerland)
- ✓ this result is a special case of quantum statistical comparison: powerful link between statistics and dynamics (quantum thermodynamics, quantum resource theories, quantum information theory, measurements (in)compatibility, etc)



Robustness of semiquantum games against classical communication

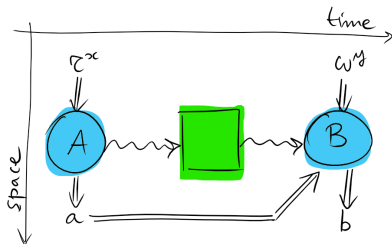
- ✓ any Bell test is spoiled, as soon as one player can communicate with the other one
- ✓ \implies Bell tests cannot verify quantum channels
- ✓ Rosset et al., 2013: there exist semiquantum games that are robust against unlimited classical communication (in fact, up to any SEPP protocol)
- ✓ this feature is especially welcome in the time-like scenario, where signaling cannot be ruled out and hence *must be assumed*



$$p(a, b|x, y) = \text{Tr} \left[(P_{\text{LOCC}}^{ab}) (\tau_{A'}^x \otimes \rho_{AB} \otimes \omega_{B'}^y) \right]$$

(LOCC w.r.t. $A'A \leftrightarrow BB'$)

Time-like semiquantum games



- ✓ give Alice a state τ^x at time t_0
- ✓ wait some time
- ✓ give her another state ω^y at time t_1
- ✓ the round ends with Alice outputting an outcome b

(here we should think of B as “Alice after some time”)

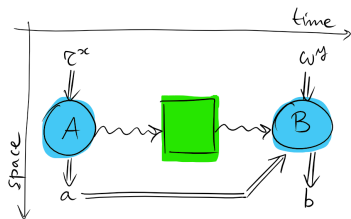
the input/output correlation is computed as

$$p(b|x, y) = \sum_a \text{Tr} \left[P_{BA}^{b|a} \{ \omega_B^y \otimes \mathcal{E} \circ \mathcal{I}^a(\tau_A^x) \} \right]$$

where $\{\mathcal{I}^a\}$ is an instrument, so that **any amount of classical communication can be transmitted** through the index a

Features of time-like semiquantum games

- ✓ as long as the quantum memory (channel) \mathcal{E} is not entanglement breaking, there exists a time-like semiquantum game capable of certifying that
- ✓ assumption: we need to trust the preparation of states τ^x and ω^y , but that is anyway required in the time-like scenario (no fully device-independent quantum channel verification [Pusey, 2015])
- ✓ \implies faithfulness with minimal assumptions
- ✓ extra feature: it is possible to quantify the minimal dimension of the quantum memory



Conclusions

- ✓ entanglement witnesses: **faithful**, but **complete trust is necessary**
- ✓ Bell tests: **fully device-independent**, but **not faithful**
- ✓ **semiquantum tests**: **faithful**, and **trust is required only for the referee's preparation devices**
- ✓ semiquantum tests are particularly compelling in the time-like scenario, in which no device-independent quantum channel verification exists anyway
- ✓ \implies **verification of non-classical correlations among any two locally quantum agents, independent of their causal separation**
- ✓ the test is **quantitative**: a lower bound on the quantum dimension can be given



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